

Section 1.5

What was done in 2 and 3 dimensions is extended to n dimensions

Matrix multiplication is introduced.

On page 60 the book is not clear what \mathbb{R}^n is. They call it Euclidean space.

Definitions:

Standard basis

Dot product = inner product

Length = norm of a vector

Use $\|x\|^2 = x \cdot x$ in exercise 2a

Straightforward results in Theorem 3.

Theorem 4 (Cauchy-Schwarz inequality)

$$|x \cdot y| \leq \|x\| \|y\|$$

Theorem 5 (Triangle inequality)

$$\|x + y\| \leq \|x\| + \|y\|$$

What we learn about matrices:

Matrix addition

Multiplying a matrix by a scalar

Matrix multiplication

Identity matrix I_n

Inverse of a matrix

Determinant of a matrix

$$\begin{bmatrix} 1 & & 0 \\ & \ddots & \\ 0 & & 1 \end{bmatrix}$$

Properties:

$$I_n A = A I_n$$

$$(AB)C = A(BC)$$

$A(3B + 2C) = 3AB + 2AC$ and similar the other way round

Theorem that is not proved:

If A is a square matrix then A is invertible if and only if $\text{Det } A \neq 0$.